## N5 RELATIONSHIPS 1.1

This resource is to support pupils in passing the appropriate National 5 Assessment Standard. The questions and marking schemes used are from SQA past papers and as such test the topics in their entirety from grade $A$ to $C$ and may include other areas from the course.

In addition the questions from Paper $1(P 1)$ should be completed without the use of a calculator and questions from Paper 2 (P2) permit the use of a calculator.

Each Assessment Standard is used to ensure pupils have the minimum competency on the specified sub-skills for the National 5 course. As such each Assessment Standard will test grade C work on that specific topic.

This resource is divided into two sections:

- Section A has an example on each sub skill for the relevant Assessment Standard and the marking scheme for these questions
- Section B has extra practice questions on this Assessment Standard and the marking scheme for these questions

| Unit Assessment <br> Standard | Sub skills | Section A - Question Number |
| :--- | :--- | :--- |
| Relationships <br> 1.1 | determining the equation of a <br> straight line given the gradient | Q1 |
| Applying <br> algebraic skills with linear equations or <br> inequations <br> to linear <br> equations | working with simultaneous <br> equations | Q2 (equation) |
| changing the subject of a formula |  |  |$\quad$ Q5 | Q4 |
| :--- |

## FORMULAE LIST

The roots of $a x^{2}+b x+c=0$ are $x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

Sine rule:

$$
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}
$$

Cosine rule:

$$
a^{2}=b^{2}+c^{2}-2 b c \cos A \text { or } \cos A=\frac{b^{2}+c^{2}-a^{2}}{2 b c}
$$

Area of a triangle:

$$
A=\frac{1}{2} a b \sin C
$$

Volume of a sphere:

$$
V=\frac{4}{3} \pi r^{3}
$$

Volume of a cone:

$$
V=\frac{1}{3} \pi r^{2} h
$$

Volume of a pyramid:

$$
V=\frac{1}{3} A h
$$

Standard deviation: $\quad s=\sqrt{\frac{\Sigma(x-\bar{x})^{2}}{n-1}}=\sqrt{\frac{\Sigma x^{2}-(\Sigma x)^{2} / n}{n-1}}$, where $n$ is the sample size.

## Section A

## Section A

| Q |  | Marks |
| :---: | :---: | :---: |
| $\begin{aligned} & \text { 1 } \\ & \text { P1 } \end{aligned}$ | 6. A taxi fare consists of a $£ 2$ "call-out" charge plus a fixed amount per kilometre. <br> The graph shows the fare, $f$ pounds for a journey of $d$ kilometres. <br> The taxi fare for a 5 kilometre journey is $£ 6$. <br> Find the equation of the straight line in terms of $d$ and $f$. | $\begin{array}{\|l\|} \hline 4 \\ \hline(2.1) \end{array}$ |
| $\begin{aligned} & \mathbf{2} \\ & \text { P1 } \end{aligned}$ | 4. Solve the equation $3 x+1=\frac{x-5}{2} .$ | 3 |
| $\begin{aligned} & \hline 3 \\ & \text { P1 } \end{aligned}$ | (b) Solve the inequality $4 x-5 \leq 7 x-20 .$ <br> 7. | 3 |
| $\begin{aligned} & 4 \\ & \text { P1 } \end{aligned}$ | 11. (a) A cinema has 300 seats which are either standard or deluxe. <br> Let $x$ be the number of standard seats and $y$ be the number of deluxe seats. <br> Write down an algebraic expression to illustrate this information. <br> (b) A standard seat costs $£_{4} 4$ and a deluxe seat costs $£ 6$. <br> When all the seats are sold the ticket sales are $£ 1380$. <br> Write down an algebraic expression to illustrate this information. <br> (c) How many standard seats and how many deluxe seats are in the cinema? | 1 <br> (2.1) <br> 2 <br> (2.1) <br> 3 <br> (2.2) |

N5 - REL 1.1 - Remediation
P1
$\square$

## Section A - Marking Scheme



| 7 | b | Solve the inequality $4 x-5 \leq 7 x-20$ <br> Ans: $x \geq 5$ or $5 \leq x$ <br> - ${ }^{1}$ dealing with variable <br> - ${ }^{2}$ dealing with constant <br> -3 solution | 3 $(\mathrm{KU})$ | -1 | $-3 x \text { or } 3 x$ <br> -15 or 15 $x \geq 5 \text { or } 5 \leq x$ |
| :---: | :---: | :---: | :---: | :---: | :---: |

4



## Section B

## Section B

Paper 1 Questions

| Q |  | Marks |
| :---: | :---: | :---: |
| 1 | 3. $W=B H^{2}$ <br> Change the subject of the formula to $H$. | 2 |
| 2 | 4. A straight line cuts the $x$-axis at the point $(9,0)$ and the $y$-axis at the point $(0,18)$ as shown. <br> Find the equation of this line. | 3 |
| 3 | 6. Jane enters a two-part race. <br> (a) She cycles for 2 hours at a speed of $(x+8)$ kilometres per hour. Write down an expression in $x$ for the distance cycled. <br> (b) She then runs for 30 minutes at a speed of $x$ kilometres per hour. Write down an expression in $x$ for the distance run. <br> (c) The total distance of the race is 46 kilometres. Calculate Jane's running speed. | 1 <br> (2.1) <br> 1 <br> (2.1) <br> 3 <br> (2.2) |


| 4 | 8. In triangle PQR : <br> - $\mathrm{PQ}=x$ centimetres <br> - $\mathrm{PR}=5 x$ centimetres <br> - $\mathrm{QR}=2 y$ centimetres. <br> (a) The perimeter of the triangle is 42 centimetres. <br> Write down an equation in $x$ and $y$ to illustrate this information. <br> (b) PR is 2 centimetres longer than QR . <br> Write down another equation in $x$ and $y$ to illustrate this information. <br> (c) Hence calculate the values of $x$ and $y$. | 2 <br> (2.1) <br> 2 <br> (2.1) <br> 3 |
| :---: | :---: | :---: |
| 5 | 9. A formula used to calculate the flow of water in a pipe is $f=\frac{k d^{2}}{20} .$ <br> Change the subject of the formula to $d$. | 3 |
| 6 | 3. Change the subject of the formula to $s$. $t=\frac{7 s+4}{2}$ | 3 |


| 7 | 7. A straight line has equation $y=m x+c$, where $m$ and $c$ are constants. <br> (a) The point $(2,7)$ lies on this line. <br> Write down an equation in $m$ and $c$ to illustrate this information. <br> (b) A second point $(4,17)$ also lies on this line. <br> Write down another equation in $m$ and $c$ to illustrate this information. <br> (c) Hence calculate the values of $m$ and $c$. <br> (d) Write down the gradient of this line. | 1 <br> (2.1) <br> 1 <br> (2.1) <br> 3 <br> 1 <br> (2.2) |
| :---: | :---: | :---: |
| 8 | 9. Part of the graph of the straight line with equation $y=\frac{1}{3} x+2$, is shown below. <br> (a) Find the coordinates of the point B. <br> (b) For what values of $x$ is $y<0$ ? | $\begin{aligned} & 2 \\ & (2.1) \\ & 1 \end{aligned}$ |

9 11. Two triangles have dimensions as shown.

| 10 7. (a) Brian, Molly and their four children visit Waterworld. |
| :--- | :--- | :--- | :--- |
| The total cost of their tickets is $f_{5} 56$. |

12 8. The graph below shows two straight lines.

- $y=2 x-3$
- $x+2 y=14$


The lines intersect at the point P .
Find, algebraically, the coordinates of $P$.
13
9. Each day, Marissa drives 40 kilometres to work.
(a) On Monday, she drives at a speed of $x$ kilometres per hour.

Find the time taken, in terms of $x$, for her journey.
(b) On Tuesday, she drives 5 kilometres per hour faster.

Find the time taken, in terms of $x$, for this journey.
(c) Hence find an expression, in terms of $x$, for the difference in times of the two journeys.
Give this expression in its simplest form.
14 4. Change the subject of the formula to $r$.

$$
A=4 \pi r^{2}
$$

15 6. Joan buys gold and silver charms to make bracelets.
2 gold charms and 5 silver charms cost $£ 125$.
(a) Let $g$ pounds be the cost of one gold charm and $s$ pounds be the cost of one silver charm.

Write down an equation in terms of $g$ and $s$ to illustrate the above information.

4 gold charms and 3 silver charms cost $£ 145$.
(b) Write down another equation in terms of $g$ and $s$ to illustrate this information.
(c) Hence calculate the cost of each type of charm.


Which one of these above could represent the line with equation $2 x+y=3$ ?
Give two reasons to justify your answer.
17
9. Quick-Smile photographers charge the following rates:

- 50 p per photograph for the first 12 photographs printed
- 35 p per photograph for any further photographs printed
- $£ 4 \cdot 25$ for a CD of the photographs.
(a) How much will it cost to have 16 photographs printed plus a CD?
(b) Find a formula for C , the cost in pounds, of having $x$ photographs printed (where $x$ is greater than 12) plus a CD.


## 18 11. (a) A straight line has equation $4 x+3 y=12$.

Find the gradient of this line.

## Paper 2 Questions

| Q |  | Marks |
| :---: | :---: | :---: |
| 19 | 4. Solve the inequality $\frac{x}{4}-\frac{1}{2}<5 .$ | 2 |
| 20 | 4. Aaron saves 50 pence and 20 pence coins in his piggy bank. <br> Let $x$ be the number of 50 pence coins in his bank. <br> Let $y$ be the number of 20 pence coins in his bank. <br> (a) There are 60 coins in his bank. <br> Write down an equation in $x$ and $y$ to illustrate this information. <br> (b) The total value of the coins is $£ 17 \cdot 40$. <br> Write down another equation in $x$ and $y$ to illustrate this information. <br> (c) Hence find algebraically the number of 50 pence coins Aaron has in his piggy bank. | 1 <br> (2.1) <br> 1 <br> (2.1) <br> 3 <br> (2.2) |

21 10. To hire a car costs $£_{\mathrm{J}} 25$ per day plus a mileage charge.
The first 200 miles are free with each additional mile charged at 12 pence.

## CAR HIRE <br> £25 per day

- first 200 miles free
- each additional mile only 12 p
(a) Calculate the cost of hiring a car for 4 days when the mileage is 640 miles.
(b) A car is hired for $d$ days and the mileage is $m$ miles where $m>200$.

Write down a formula for the cost $£ C$ of hiring the car.
22 6. Teams in a quiz answer questions on film and sport.
This scatter graph shows the scores of some of the teams.
sport
score


A line of best fit is drawn as shown above.
(a) Find the equation of this straight line.
(b) Use this equation to estimate the sport score for a team with a film score of 20 .

23 10. Tom and Samia are paid the same hourly rate.
Harry is paid $\frac{1}{3}$ more per hour than Tom.
Tom worked 15 hours, Samia worked 8 hours and Harry worked 12 hours.
They were paid a total of $£ 429$.
How much was Tom paid?
24 10. A taxi fare consists of a call-out charge of $£ 1 \cdot 80$ plus a fixed cost per kilometre.
A journey of 4 kilometres costs $£ 6 \cdot 60$.
The straight line graph shows the fare, $f$ pounds, for a journey of $d$ kilometres.

(a) Find the equation of the straight line.
(b) Calculate the fare for a journey of 7 kilometres.

25 3. Two groups of people go to a theatre.
Bill buys tickets for 5 adults and 3 children.
The total cost of his tickets is $£ 158 \cdot 25$.
(a) Write down an equation to illustrate this information.
(b) Ben buys tickets for 3 adults and 2 children.

The total cost of his tickets is $£ 98$.
Write down an equation to illustrate this information.
(c) Calculate the cost of a ticket for an adult and the cost of a ticket for a child.
11. Change the subject of the formula $s=u t+\frac{1}{2} a t^{2}$ to $a$.


## Section B - Marking Scheme

## Marking Scheme

## Paper 1




N5 - REL 1.1 - Remediation


N5 - REL 1.1 - Remediation

| 5 | NOTES: <br> (i) <br> (ii) <br> (iii) | Ans: $\quad d=\sqrt{\frac{20 f}{k}}$ <br> - beginning to rearrange <br> - continuing rearrangement <br> - completed rearrangement <br> for $d=\sqrt{\frac{20 f}{k}}$, with or without working <br> for $d=\frac{\sqrt{20 f}}{k}$, with or without working the $3^{\text {rd }}$ mark is for the square root of the $c$ | - $k d^{2}=20 f$ <br> - $d^{2}=\frac{20 f}{k}$ <br> - $d=\sqrt{\frac{20 f}{k}}$ <br> date's expression for $d^{2}$ | 3 KU <br> award $3 / 3$ <br> award $2 / 3$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 6 | 3 | Ans: $s=\frac{2 t-4}{7}$ <br> - beginning to rearrange <br> - continuing to rearrange <br> - completed rearrangement | - $7 s+4=2 t$ <br> - $7 s=2 t-4$ <br> - $s=\frac{2 t-4}{7}$ | 3KU |  |

N5 - REL 1.1 - Remediation



N5 - REL 1.1 - Remediation


N5 - REL 1.1 - Remediation


N5 - REL 1.1 - Remediation


(16



## Paper 2



N5 - REL 1.1 - Remediation


N5 - REL 1.1 - Remediation

| 23 | 10 | Ans: £165 <br> - Valid strategy involving $\frac{1}{3}$ <br> - Creating an equation <br> - solution | - $12+\frac{1}{3}(12)$ or $x+\frac{1}{3} x$ <br> - $15+8+16=39$ <br> Or <br> - $15 x+8 x+12\left(\frac{4}{3} x\right)=39 x$ <br> - $\frac{429}{39} \times 15=£ 165$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | 3 KU |

NOTES:
(i) the final mark is for obtaining an hourly rate $\times 15$
eg $15+8+12=35$
$\frac{429}{35} \times 15=£ 183.86$

N5 - REL 1.1 - Remediation


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| Question |  | Expected Answer(s) <br> Give one mark for each • | Max <br> Mark | Illustrations of evidence for <br> awarding a mark at each |
| :--- | :--- | :--- | :--- | :--- |
| 3. | (a) | Ans: $5 a+3 c=158 \cdot 25$ <br> $\bullet$ •1 construct equation | 1 |  |
| Notes: |  |  | $\bullet^{1} 5 a+3 c=158 \cdot 25$ |  |

1. Accept variables other than $a$ and $c$.

| (b) | Ans: $3 a+2 c=98$ <br> $\bullet$ construct equation | 1 |  |
| :--- | :--- | :--- | :--- | :--- |

Notes:

| (c) | Ans: Adult ticket costs $£ 22.50$ Child ticket costs $£ 15 \cdot 25$ <br> - ${ }^{1}$ evidence of scaling <br> $\bullet^{2}$ follow a valid strategy through to produce values for $a$ and $c$ <br> - ${ }^{3}$ calculate correct values for $a$ and $c$ <br> - ${ }^{4}$ communicate answers in money | 4 | $\begin{aligned} \cdot 1 \mathrm{eg} 10 a+6 c & =316 \cdot 50 \\ 9 a+6 c & =294 \end{aligned}$ <br> - ${ }^{2}$ values for $a$ and $c$ <br> - ${ }^{3} a=22.5$ and $c=15.25$ <br> - ${ }^{4}$ Adult $£ 22 \cdot 50$ Child $£ 15.25$ |
| :---: | :---: | :---: | :---: |

## Notes:

1. The fourth mark may only be awarded when all of the following are given in the final answer: the words "adult" and "child", the $£$ signs and both amounts written with two decimal figures.
26

2. For subsequent incorrect working, the final mark is not available.
3. For $a=\frac{s-u t}{\frac{1}{2} t^{2}}$ award 2/3
