## N4 EXPRESSIONS & FORMULAE 1.1

This resource is to support pupils in passing the appropriate National 4
Assessment Standard. The questions and marking schemes used are from SQA
past papers and as such test the topics in their entirety from grade A to C and
may include other areas from the course. In addition the questions from
Paper 1 (P1) should be completed without the use of a calculator and
questions from Paper 2 (P2) permit the use of a calculator.

Each Assessment Standard is used to ensure pupils have the minimum competency on the specified sub-skills for the National 4 course. As such each Assessment Standard will test grade C work on that specific topic.

This resource is divided into two sections:

- Section A has an example on each sub skill for the relevant Assessment Standard and the marking scheme for these questions
- Section B has extra practice questions on this Assessment Standard and the marking scheme for these questions

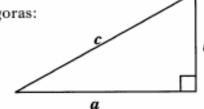
Unit Assessment Standard	Sub skills	Section A – Question Number
Expressions & Formulae 1.1	The sub-skills are: using the distributive law in an expression with a numerical common factor to produce a sum of terms	Q1
Applying algebraic skills to	factorising a sum of terms with a numerical common factor	Q2
manipulating expressions and	simplifying an expression which has more than one variable	Q3
working with formulae	evaluating an expression or a formulae which has more than one variable	Q4
	extending a straightforward number or diagrammatic pattern and determining its formula	Q5
	calculating the gradient of a straight line from horizontal and vertical distances	Q6

#### FORMULAE LIST

Circumference of a circle:  $C = \pi d$ Area of a circle:  $A = \pi r^2$ Curved surface area of a cylinder:  $A = 2\pi rh$ Volume of a cylinder:  $V = \pi r^2 h$ 

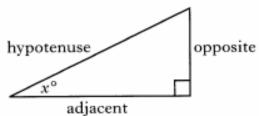
Volume of a triangular prism: V=Ah

Theorem of Pythagoras:



$$a^2 + b^2 = c^2$$

Trigonometric ratios in a right angled triangle:

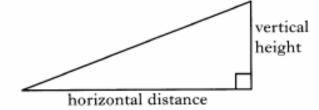


$$tan x^{\circ} = \frac{opposite}{adjacent}$$

$$sin x^{\circ} = \frac{opposite}{hypotenuse}$$

$$cos x^{\circ} = \frac{adjacent}{hypotenuse}$$

Gradient:



## Section A

Q		Marks
Q1 P2	5. (a) Multiply out the brackets and simplify	2
	5(2m+7)-m.	
Q2	Factorise 12t + 9u	2
P2		
Q3	Simplify 3d + 4f – d + 6f	1
Q4 P1	9. Evaluate $2gh - w$ when $g = -10$ , $h = 4$ and $w = -30$ .	3
Q5 P1	6. A children's play area is to be fenced.  The fence is made in sections using lengths of wood, as shown below.	
	1 section	
	2 sections	
	3 sections	
	(a) Complete the table below.	
	Number of sections (s) 1 2 3 4 5 12	2
	Number of lengths of wood (w) 6 11	_
	(b) Write down a formula for calculating the number of lengths of wood (w), when you know the number of sections (s).	2
	(c) A fence has been made from 81 lengths of wood.  How many sections are in this fence?  You must show your working.	2
Q6	Find the gradient of the line AB when A (2,6) and B(6,14)	2

## Section A

# MARKING SCHEME

#### **Section A - Marking Scheme**

Q						Marks
Q1	Que	estion	Expected Answer/s	Max	Additional Guidance	2
	5	а	Ans: 9m + 35  1 multiply out bracket: 10m + 35  2 collect like terms: 9m + 35	Mark 2	<ol> <li>Correct answer without working award 2/2</li> <li>2<sup>nd</sup> mark is not available if there is invalid subsequent working eg 9m + 35 → 44m award 1/2 9m + 35 → 35/9 award 1/2</li> <li>10m + 35 - 5m = 5m + 35 ×√ award 1/2</li> </ol>	
Q2	(b)	An	is: $3(4t + 3u)$			2
		•1	correct factorisation		3( )  or  (4t + 3u) 3(4t + 3u) <b>2K</b>	
Q3	2d	+ 10	f			1

Question	Expected Answer/s	Max Mark	Additional Guidance
9	Ans: -50  In the integers of t	3	<ol> <li>Correct answer without working award 2/3</li> <li>2nd mark is only available for correctly multiplying at least three of the numbers 2, -10, 4 and -30.</li> <li>Some common answers         <ul> <li>(a) -80 award 2/3 √√x</li> <li>(b) -80-30 = -50 award 2/3 √√x</li> <li>(c) -80-30 = -110 award 2/3 √√x</li> <li>(d) 2 × (-10) × 4 = 80→80-(-30) = 110 award 2/3 √x√x</li> <li>(e) 2 × 10 × 4 = 80→80-(-30) = 110 award 1/3 × x√x</li> <li>(f) 2 × (-10) + 2 × 4 = -12 award 0/3</li> </ul> </li> </ol>
6 (a) (b)	Ans: $ \begin{array}{c cccc} 1 & 2 & 3 & 4 & 5 \\ \hline 6 & 11 & 16 & 21 & 26 \end{array} $ • Any 2 correct lengths of • 2 further correct lengths  Ans: $w = 5s + 1$ • ${}^{1}\& {}^{2}$ Correct formula	wood	•1 Any 2 from 16, 21, 26, 61 •2 Remaining 2 from 16, 21, 26, 61  2R •1&•2 $w = 5s + 1$
(c)	Ans: $s = 16$ • Correct strategy to find $s$ • Correct solution		$\bullet^{1} \qquad 81 = 5s + 1$ $\bullet^{2} \qquad s = 16$ 2R

Notes:

In part (b)

- (i) For an answer of (=) 5s + 1 award 1/2
- (ii) Do not penalise bad form eg w = 6s (s 1)
- (iii) A formula in words is not acceptable
- (iv) For s = 5w + 1 award 0/2

In part (c)

- (i) Solution may be obtained by extending the table
- (ii) For a final answer of 16 without working award 0/2
- (iii) For  $81 \div 5 = 16(\cdot 2)$  award 1/2

Q6

• 1 mark for using

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{14 - 6}{6 - 2} = \frac{8}{4} = 2$$

• 1 mark for correct answer

Note: 1/2 for gradient of  $\frac{1}{2}$ .

2

## Section B

#### Section B – Paper 1 – Questions

Q		Marks
1	3. Samira is designing a chain belt.  Each section of the belt is made from metal rings as shown below.	
	1 section, 4 rings	
	2 sections, 9 rings	
	(a) Complete the table below.	
	Number of sections (s) 1 2 3 4 5 11	2
	Number of metal rings (r) 4 9	2
	(b) Write down a formula for calculating the number of rings (r), when you know the number of sections (s).	
		2
	(c) Samira uses 79 rings to make her belt.  How many sections does her belt have?	2

2	Simplify	8t + 2s - 3t + s - 4t	1
3	Simplify	9n + 8m – 10n + m	1
4	Simplify	7a – 3b + 4a + 9b	1

#### Section B – Paper 2 – Questions

Q		Marks
5	4. Mhairi makes necklaces in M-shapes using silver bars.	
	(a) Complete the table below.	
	Number of M-shapes (m) 1 2 3 4 15	
	Number of bars (b) 4 7	2
	(b) Write down a formula for calculating the number of bars (b) when you know the number of M-shapes (m).	2
		2
	(c) Mhairi has 76 silver bars.  How many M-shapes can she make?	2

6	6. (a) Simplify	
	8(c-3) + 5(c+2).	3
7	8. (b) Factorise fully	
	20x - 12y.	2
8	5. (a) Factorise	2
	6c - 15d. (b) Simplify	
	5(a+1) + 2(5-2a).	2
9	3. Multiply out the brackets and simplify	
	4(2-3x) + 5(4x+1).	3
10	4. Factorise	
	15a + 12.	2
11	2. (a) Multiply out the brackets and simplify	2
	6(2n-3)+11.	2
	(b) Factorise	
	20s + 45.	2
12	10. Use the formula below to find the value of S when $n = 25$ , $a = 1.5$ , and $L = 6.3$ .	
	$S = \frac{n(a+L)}{2}$	3

### Section B

## NARKING SCHEME

#### Section B – Paper 1 – Marking Scheme

Q	Г	Marks
1		
	3 (a) Ans:	
	Number of sections (s) 1 2 3 4 5 11	
	Number of metal rings (r)   4   9   14   19   24   54	
	•¹ any two correct number of rings •¹ any two from 14, 19, 24, 54	
	•² two further correct number of rings remaining two from 14, 19, 24, 54	
	2R 2	2
	(b) Ans: $r = 5s - 1$	
	•1+2 correct formula $•1+2 r = 5s - 1$	
	2R 2	2
	(c) Ans: 16	
	•¹ correct strategy to find $s$ •¹ $79 = 5s - 1$	
	• correct solution $\bullet^2  s = 16$	
	2R	2
	NOTES: (b) for (:) 5s-1 award 1/2	
	(c) solution may be obtained by extending table	
2		1
3		1
4	11a + 6b	1

#### Section B – Paper 2 – Marking Scheme

Q			Marks
5	1 (2)	Ann. 10 12 46	
	4 (a)	Ans: 10, 13, 46	
		•¹ Two entries correct •¹ e.g. 10, 13	
		• A further entry correct • e.g. 46	2
	(b)	Ans: $b = 3m + 1$	-
		• $^{1}$ &• $^{2}$ Correct formula • $^{1}$ &• $^{2}$ $b=3m+1 $	2
	(c)	Ans: 25	_
		• Correct strategy to find $b$ • $3m + 1 = 76$	
		• Correct solution • 2 25	2
	Notes:		-
	In part (b)	<ul> <li>(i) For an answer of (=) 3m + 1 - award 1/2</li> <li>(ii) Do not penalise bad form e.g. b = 4m - (m - 1)</li> <li>(iii) A formula in words is not acceptable</li> <li>(iv) For m = 3b + 1 - award 0/2</li> </ul>	
	In part (c)	<ul> <li>(i) Solution may be obtained by extending the table</li> <li>(ii) For a final answer of 25 without working – award 2/2</li> <li>(iii) For 76 ÷ 3 = 25(.3) – award 1/2</li> <li>(iv) For 76 × 3 + 1 = 229 – award 0/2</li> </ul>	

6 (a)	Ans: 13c-14  1 correct expansion of 1st bracket  2 correct expansion of 2nd bracket  3 correct simplification	- 121
5 (a)	Ans: $3(2c - 5d)$ • 1 correct common factor  • 2 correct factorisation  • 2	$a^{1}  3 \ ()$ $a^{2}  (2c-5d)$
(b)	1st bracket  • 2 correct multiplication of 2nd bracket	$a \cdot 1 = 5a + 5$ $a \cdot 2 = 10 - 4a$ $a \cdot 3 = a + 15$
	5 (a)	•¹ correct expansion of 1st bracket  •² correct expansion of 2nd bracket  •³ correct simplification  5 (a) Ans: 3(2c - 5d)  •¹ correct common factor  •² correct factorisation  (b) Ans: a + 15  •¹ correct multiplication of 1st bracket  •² correct multiplication of 2nd bracket

8	8.		
	(b)  Note: (ii) I	Ans: $4(5x - 3y)$ • Finds one correct factor  • Ansight of the second	2
9	3	<ul> <li>Ans: 13 + 8x or equivalent</li> <li>1 multiply out one bracket: 8 - 12x or 20x + 5</li> <li>2 multiply out both brackets and know to add: 8 - 12x + 20x + 5</li> <li>3 collect like terms: 13 + 8x or equivalent</li> <li>3 Some common answers  (a) 13 + 32x award 2/3 ✓ ✓ × (b) 8 - 12x = 20x + 5 award 1/3 ✓ × × (c) 3rd mark is not available if there is invalid subsequent working e.g. 13 + 8x → 21x award 2/3 13 + 8x → 13/8 award 2/3</li> </ul>	3
10	4	Ans: 3(5a + 4)  • 1 identify common factor: 3 or 5a + 4  • 2  • 2	2

11						
	2	a	Ans: •¹ •²	12n - 7 multiply out bracket: 12n - 18 collect like terms: 12n - 7	2	<ol> <li>Correct answer without working award 2/2</li> <li>2<sup>nd</sup> mark is not available if there is invalid subsequent working eg         12n - 7 → 5n award 1/2         12n - 7 → 7/12 award 1/2     </li> </ol>
	2	b	Ans: •¹ •²	5(4s + 9) identify common factor: 5 or 4s + 9 factorise: 5(4s + 9)	2	1. 20(s + 2·25), 10(2s + 4·5) award 1/2
12	10		Ans: •¹ •² •³	know how to evaluate numerator: $25 \times (1.5 + 6.3)$ or $25 \times 1.5 + 25 \times 6.3$ evaluate numerator: 195 divide numerator by 2 correctly: $195 \div 2 = 97.5$	3	1. Correct answer without working award 3/3  2. Some common answers (working must be shown)  (a) 116·25 [(25 × 1·5) +(25 × 6·3) ÷ 2 = 37·5 + 157·5 ÷ 2 = 37·5 + 78·75]  award 2/3 ✓ ✓ ×  (b) 48·75 [(25 × 7·8) ÷ 2 = 12·5 × 3·9]  award 2/3 ✓ ✓ ×  (c) 21·9 [(25 × 1·5 + 6·3) ÷ 2]  award 2/3 × ✓ ✓  (d) 40·65 [25 × 1·5 + 6·3 ÷ 2]  award 1/3 × ✓ ×  (e) 16·4 [(25 + 1·5 + 6·3) ÷ 2]  award 1/3 × × ✓  (f) 118·125 [25 × 1·5 × 6·3 ÷ 2]  award 0/3  (g) 29·65 [25 + 1·5 + 6·3 ÷ 2]  award 0/3